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TEST ID: 50 PHYSICS

4.THERMODYNAMICS

Single Correct Answer Type

1. A gas is expanded from volume V_0 to $2V_0$ under three different processes shown in figure. Process 1 is isobaric process, process 2 is isothermal and process 3 is adiabatic. Let $\Delta U_1, \Delta U_2$ and ΔU_3 be the change in internal energy of the gas in these three processes. Then,



a) $\Delta U_1 > \Delta U_2 > \Delta U_3$ b) $\Delta U_1 < \Delta U_2 < \Delta U_3$ c) $\Delta U_2 < \Delta U_1 > \Delta U_3$ d) $\Delta U_2 < \Delta U_3 < \Delta U_1$

2. In which thermodynamic process, the change in internal energy ' Δ U', heat supplied 'Q' and the work done in expansion 'W' are all non-zero?

a) Adiabatic	b) Isobaric
c) Isothermal	d)Isochoric

3. In the indicator diagram, T_a, T_b, T_c, T_d represents temperatures of gas at A, B, C, D respectively. Which of the following is correct relation?



a) $T_a = T_b = T_c = T_d$ b) $T_a \neq T_b \neq T_c \neq T_d$ c) $T_a = T_b$ and $T_c = T_d$ d) None of these

4. The specific heat of hydrogen gas at constant pressure is $C_p = 3.4 \times 10^3 \text{ cal/kg}^\circ \text{C}$ and at constant volume is $C_V = 2.4 \times 10^3 \text{ cal/kg}^\circ \text{C}$. If 1 kg hydrogen gas is heated from 10°C to 20°C at constant pressure, the external work done on the gas to maintain it at constant pressure is

a) 10 ⁶ cal	b) 10 ⁴ cal	
c) 10 ³ cal	d) 5×10^3 cal	
The initial pressure and volume of a gas is 'P'		
1 (17)	I Phase Lands and Lands	

5. The initial pressure and volume of a gas is 'P' and 'V' respectively. First by isothermal process gas is expanded to volume '9V' and then by adiabatic process its volume is compressed to 'V' then its final pressure is (Ratio of specific heat at constant pressure to constant volume= $\frac{3}{2}$)

a) 6P b) 27P c) 3P d) 9P

6. Six moles of O₂ gas is heated from 20°C to 35°C at constant volume. If specific heat capacity at constant pressure is 8 cal mol⁻¹ K⁻¹ and R = 8.31Jmol⁻¹ K⁻¹, what is change in internal energy of gas?
a) 180 cal
b) 300 cal

,	,
c) 360 cal	d)540 cal

- 7. An ideal gas expands adiabatically, $(\gamma = \frac{3}{2})$. To reduce the r. m. s. velocity of the molecules 3 times the gas has to be expanded a) 81 times b) 18 times c) 9 times d) 27 times
- 8. A cylinder of fixed capacity (of 44.8 L) contains 2 moles of helium gas at STP. What is the amount of heat needed to raise the temperature of the gas in the cylinder b 20° C? (Take , $R = 8.31 \text{ J mol}^{-1} \text{ k}^{-1}$)

a) 996 J	b)831 J
c) 498 J	d)374 J

 A gas is compressed at a constant pressure of 50 Nm⁻² from a volume of 10 m³ to a volume of 4 m³. Energy of 100 J added to gas by heating. Its internal energy is

a) Increased by 400 J b) Increased by 200 J c) Increased by 100 J d) Decreased by 200 J

10. A sample of 0.1 g of water at 100° C and normal pressure (1.013×10^{5} Nm⁻²) requires 54 cal of heat energy to convert to steam at 100° C. If the volume of the steam produced is 167.1 cc, the change in internal energy of the sample, is a) 42.2 J b) 208.8 J



d) Temperature of the system changes during the process 18. The internal energy of a gas contained in a movable box moving with a constant speed v b) Does not depend on d)Both (b) and (c) 19. In a certain process, 400 cal of heat is supplied to a system and at the same 105 J of mechanical work was done on the system. The increase in its internal energy is b) 303 cal d)425 cal 20. At 27^o C, a motor car tyre has pressure of 2 atm. The temperature at which the tyre

b) 8P₀

d) $16P_0$

the process

- suddenly burst will be (given , $\gamma_{air} = 1.4$) b)250 K d)248 K 21. An ideal gas is expanded adiabatically. How
- many times has the gas to be expanded to reduce the rms speed of molecules 2 times?
 - b)4 times d)8 times
- 22. A gas expands adiabatically at constant pressure, such that its temperature T $\propto \frac{1}{\sqrt{N}}$. The value of C_p/C_V of the gas is b) 1.50
- d)2.00 23. An ideal gas ($\gamma = 1.5$) is expanded
- adiabatically. How many times has the gas to

be expanded to reduce r. m. s. velocity of molecules two times?

a) 8 times	b) 16 times
c) 12 times	d)20 times

24. 1 mole of an ideal monoatomic gas is heated at a constant pressure of 1 atmosphere from 0°C to 100°C. Work done by the gas is

a)
$$8.31 \times 10^3$$
 J b) 8.31×10^{-3} J

- d) 8.31×10^2 J c) 8.31×10^{-2} J
- 25. An ideal gas which is diatomic $\left(\gamma = \frac{7}{5}\right)$ undergoes an adiabatic change. If the relation between temperature and volume is $TV^{x} =$ constant, then the value of x is

a) $\frac{1}{3}$	b) $\frac{2}{5}$
$(1)^{\frac{3}{2}}$	$d) = \frac{1}{2}$
3	⁴ 4

- 26. Amongst the following variables, state variable is (are)
 - a) Heat b)Work c) Internal energy d)All of these
- 27. Following figure shows two processes A and B for a gas. If ΔQ_A and ΔQ_B are the amount of heat absorbed by the system in two cases and ΔU_A and ΔU_B are changes in internal energies respectively, then



28. A thermodynamic system undergoes a cyclic process ACDEA as shown in figure. Work done by the system is



	, , , , , , , , , , , , , , , , , , , ,	5 0 0
29.	29. The internal energy of a system could be	
	changed	
	a) By extracting heat	b) By doing work done
	from the system	on the system
	c) If system do some	d)All of the above
	work on the	
	surroundings	
30.	In an adiabatic proces	s, pressure is increased
by $\frac{2}{3}$ %. If $\frac{C_p}{C_V} = \frac{3}{2}$, then the volume decr		the volume decreases by
	about	
	$\frac{4}{2}$	$h)^{2}_{-\%}$
	a) <u>-</u> 70	3^{-10}

d) $2P_0V_0$

c) P_0V_0

c) 4%

- d) $\frac{9}{4}$ % 31. The graph of thermodynamic process is a straight line parallel to pressure axis in a pV diagram. The work done in this process is a) Zero b) \sqrt{pV} c) 2PV d)Infinity
- 32. If an average person jogs, he produces $14.5 \times$ 10^4 cal/min. This is removed by the evaporation of sweat. The amount of sweat evaporated per minute (assuming 1 kg requires 580×10^3 cal for evaporation) is a) 0.25 kg b) 2.25 kg c) 0.05 kg d) 0.20 kg
- 33. A monoatomic gas is suddenly compressed to $\left(\frac{1}{2}\right)$ th of its initial volume adiabatically. The ratio of the final pressure to initial pressure of the gas is (v = 5/3)

a)
$$32$$
 b) 8
c) $\frac{40}{3}$ d) $\frac{24}{5}$

34. We consider a thermodynamic system. If ΔU represents the increase in its internal energy and W is the work done by the system, which of the following statements are true?

	0	
_]	$\Delta U = -W$ is an	$\Delta U = W$ in an
aj	adiabatic process.	isothermal process.
പ	$\Delta U = -W$ in an	$\Delta U = W$ in an
CJ	isothermal process.	adiabatic process.

- 35. If in a thermodynamic system, ' ΔU ' represents the increase in its internal energy and 'W' is the amount of work done by the system, then which one of the following statements is true?
 - a) $\frac{\Delta U = W \text{ in an}}{\text{adiabatic process}}$ b) $\Delta U = -W$ in an isothermal process d) $\frac{\Delta U = -W \text{ in an}}{\text{adiabatic process}}$ $\Delta U = W$ in an isothermal process

- 36. In a p- V diagram for an ideal gas (where , p is along Y- axis and V is along X –axis), the value of the ratio "slope of adiabatic curve/slope of the isothermal curve" at any point will be (where symbols have their usual meanings)
 - a) 1 b) 2 c) C_p/c_v d) C_v/c_p
- 37. A gas expands with temperature according to the relation $V = kT^{2/3}$. Calculate work done when the temperature changes by 60 K. a) 10 R b) 30 R

a) 10 K	0)50 K
c) 40 R	d)20 R

38. What is the nature of change in internal energy in the following three thermodynamic processes shown in figure?



- a) $\begin{array}{l} \Delta U \text{ is positive in all} \\ \text{the three cases} \\ \Delta U \text{ is negative in all} \\ \text{the three cases} \\ \Delta U \text{ is negative for (i)} \end{array}$
- ΔU is positive for (i), c) negative for (ii), zero for (iii) $\Delta U = 0$ in all the cases
- 39. The thermodynamic process in which no work is done on or by the gas is
 - a) Isothermal process b) Isobaric process
 - c) Adiabatic process d) Isochoric process
- 40. Which one of the following equations specific an isobaric process?

 $[Q = heat supplied \Delta P, \Delta V and \Delta T are change in pressure, volume and temperature respectively]$

1 03	
a) Q = 0	b) $\Delta T = 0$
c) $\Delta V = 0$	d) $\Delta P = 0$

41. 10 moles of an ideal gas at constant temperature 500 K is compressed from 50 L to 5 L. Work done in the process is (Take, R =8.31Jmol⁻¹ K⁻¹)

a) -1.2×10^4 J	b) -2.4×10^{4} J
c) -4.8×10^4 J	d) -9.6×10^4 J

42. Out of the following statements, which one is 'NOT' correct in case of thermodynamic process?

	ي In an isothermal	In an isobaric
	^{a)} process, $\Delta T = 0$	^D process, $\Delta P = 0$
	ي In an isochoric	اn an isothermal
	$^{\rm CJ}$ process, W = 0	$^{(1)}$ process, Q \neq 0
43.	A sample of a gas exp	oands from volume 'V ₁ ' to

 V_2 '. The amount of work done by the gas is maximum when the expansion is

- a) Equal in isothermal b) Isobaric and isobaric
- c) Isothermal d) Adiabatic
- 44. A thermodynamic system is taken from state A to state B along ACB and is brought back to A along BDA as shown in figure. Net work done during one complete cycle is given by area



- a) ACBDA c) AV₁V₂BDA
 - b) ACBp₂p₁ A d) BD Ap₁p₂ B
- 45. If ' Δ U' is change in internal energy, 'W' is work done and 'Q' is amount of heat exchanged in the thermodynamic system. Match the column I with column II.

	Column		Column II	
(Isother	((i) ∆U =	
a	mal	i	–W	
)	process)		
(Isobari	($Q = \Delta U$	
b	С	i		
)	process	i		
)		
(Isochor	($\Delta U = 0$	
С	ic	i		
)	process	i		
		i		
)		
(Adiabat	($\Delta U \neq 0$	
d	ic	i		
)	process	V		
_	$(a) \rightarrow (iii)$;(b	o) (a) -	\rightarrow (i); (b) \rightarrow
a)	\rightarrow (ii); (c)	\rightarrow	(i); (d) b) (iv);	$(c) \rightarrow$
	\rightarrow (iv)		(iii)	$(d) \rightarrow (ii)$
	(a) \rightarrow (ii);	(b)	$) \rightarrow$ (a) -	\rightarrow (iii); (b) \rightarrow
c)	(iv); (c) \rightarrow	(i)	$(d) \rightarrow d(iv);$	$(c) \rightarrow (ii); (d) -$
-	(iii)		(i)	

46. Figure shows a thermodynamic process on one mole of a gas. How does the work done in the process changes with time?



- c) Only potential d) Neither kinetic nor energy potential energy
- 51. If the system is a gas in a cylinder with a movable piston as shown in the figure below, then



$$b) \left(\frac{L_1}{L_2}\right)^{2/3} \qquad b) \left(\frac{L_1}{L_2}\right) c) \left(\frac{L_2}{L_1}\right) \qquad d) \left(\frac{L_2}{L_1}\right)^{2/3}$$

56. An ideal gas of mass m in a state A goes to another state B via three different processes as shown in figure. If Q_1 , Q_2 and Q_3 denote the heat absorbed by the gas along the three paths, then



at constant pressure such that its temperature T $\propto \frac{1}{\sqrt{v}}$. The value of γ for the gas is ($\gamma = \frac{c_p}{c_v}$, V = volume of the gas) a) 1.8 b) 1.5

- c) 1.3 d) 1.4
- 58. Consider a system to be a certain mass of gas contained in a cylinder with movable piston as shown in the figure.

The state of the gas and hence its internal energy can be changed by



60. An ideal gas having pressure 'P', volume 'V' and temperature 'T' undergoes a thermodynamic process in which dW = 0 and dQ < 0. Then for the gas

a) V will increase

c) T will increase

b) P may increase or decrease

d)T will decrease

61. An ideal gas with pressure P, volume V and temperature T is expanded isothermally to a volume 2V and a final pressure P_i. The same gas is expanded adiabatically to a volume 2V, the final pressure is P_a. In terms of the ratio of the two specific heats for the gas ' γ ', the ratio $\frac{P_i}{P_a}$ is

a) $2^{\gamma+1}$ b) $2^{\gamma-1}$ c) $2^{1-\gamma}$ d) 2^{γ}

62. A system in equilibrium is divided into two equal parts. The systems before and after the divisions, with respective state variables are as shown below.



Then, from the above, we can say that

- a) U is an extensive b) T is an extensive state variable, state variable, whereas M and T are whereas U and M are intensive state intensive state variables variables
- c) U and M are d) U, M and T all are extensive state extensive state variables, whereas T variables is intensive state variable
- 63. A container of volume $1m^3$ is divided into two equal parts by partition. One part has an ideal gas at 300 K and the other part is vacuum. The whole system is thermally insulated from the surrounding. If the partition is removed, the gas expands to occupy the whole volume. The final temperature of the gas is

aj 450 K	DJ 300 K
c) 600 K	d) 150 K

64. In order to compress one kilo mole of a gas adiabatically, the work of 124 kJ is performed and in this process temperature of the gas increase by 6°C, the gas is [Universal gas constant $R = 8.3 \text{ J mol}^{-1} \text{K}^{-1}$]

- b) Rigid diatomic a) Mixture of monoatomic and triatomic gas
- c) Non rigid diatomic d) Monoatomic
- 65. In the P V diagram shown, there are two adiabatic parts of the same gas intersecting two isothermals at T_1 and T_2 . The ratio $\left(\frac{V_b}{V_2}\right)$ is equal to



- 66. Which one of the following parameters does not represent a thermodynamic state of a gas? a) Volume b)Work c) Temperature d)Pressure
- 67. A gas at pressure p is adiabatically compressed, so that its density becomes twice that of initial value. Given that $\gamma = C_p / C_v =$ 7/5, what will be the final pressure of the gas? a) 2p b) $\frac{7}{5}$ p

d)P

b)16P

c) 2.63 p

68. 'V' cc volume of a gas having $\gamma = \frac{5}{2}$ s suddenly compressed to $\left(\frac{V}{4}\right)$ c. c. The initial pressure of the gas is P. The final pressure of the gas will be

a) 32P d) $\frac{P}{16}$ c) $\frac{P}{32}$

69. Which one of the following p-V diagram is correct for an isobaric process?





70. In a thermodynamic system, 'W' represents the work done by the system and ' ΔU ' is the increase in internal energy. Which of the following statements is TRUE?

a) In an isothermal process, $\Delta U = -W$	b) In an adiabatic process, $\Delta U = W$
c) In an isothermal process, $\Delta U = W$	d) In an adiabatic process, $\Delta U = -W$

71. The p – V diagram of a system undergoing thermodynamic changes is as shown in the figure. The work done by the system in going from $A \rightarrow B \rightarrow C$ is 30 J. If 68 J of heat is given to the system, then the change in the internal energy of the system between A and C is



a) 34 J	ł	o) 55 J
c) 50 J	(ł)38 J

72. A monoatomic ideal gas initially at temperature T₁ is enclosed in a cylinder fitted with a frictionless piston. The gas is allowed to expand adiabatically to a temperature T_2 by releasing the piston suddenly. L₁ and L₂ are the lengths of the gas columns before and after the expansion respectively. Then $\frac{T_2}{T}$ is

a)
$$\left(\frac{L_2}{L_1}\right)^{2/3}$$

c)
$$\left(\frac{L_1}{L_2}\right)^{1/2}$$
 d) $\left(\frac{L_2}{L_1}\right)^{1/2}$

73. The equation of state for 2g of oxygen at a pressure 'P' and temperature 'T', when occupying a volume 'V' will be

a) $PV = \frac{1}{16} RT$ b) PV = RT

c)
$$PV = 2RT$$

74. Among given cures, which one could represent isothermal process?

d) PV = 16RT



d) None of the curves could represent isothermal process

- 75. 5 moles of an ideal gas with $\gamma = 7/5$, initially at STP is compressed adiabatically, so that its temperature becomes 400°C. The increase in the internal energy of gas in kJ is a) 21.55 b) 41.55 c) 65.55 d) 50.55
- 76. The sample of gas expands from volume ' V_1 ' to ' V_2 '. The amount of work done by the gas is greatest when the expansion is a) Adiabatic b) Isobaric
 - c) Isothermal d) Free expansion
- 77. A system is provided with 200 cal of heat and the work done by the system on the surroundings is 40 J. then , its internal energy a) Increase by 600 J b) Decrease by 800 J c) Increase by 800 J d) Decrease by 50 J
- 78. A given mass of a gas is compressed isothermally until its pressure is doubled. It is then allowed to expand adiabatically until its original volume is restored and its pressure is then found to be 0.75 of its initial pressure. The ratio of the specific heat of the gas is approximately

 a) 1.20
 b) 1.41

a) 1.20	b) 1.41
c) 1.67	d) 1.83

79. For a heat engine operating between temperatures t_1 °C and t_2 °C, its efficiency will be

a)
$$\frac{t_1 - t_2}{t_2}$$
 b) $\frac{t_1 - t_2}{t_1 + 273}$
c) $\frac{t_1}{t_2}$ d) $1 - \frac{t_2}{t_1}$

80. A system is taken through a cyclic process represented by a circle as shown in the figure. The heat absorbed by the system is



81. During an adiabatic process, the pressure of a gas is found to be proportional to the cube of its temperature. The ratio of $\frac{C_p}{C_V}$ for the gas is

a)
$$\frac{4}{3}$$
 b)2
c) $\frac{5}{3}$ d) $\frac{3}{2}$

82. An ideal gas at 27°C is compressed adiabatically to $\frac{8}{27}$ of its original volume. [TV⁻¹ = constant and $\gamma = 5/3$] Then the rise in temperature is a) 225K b) 400K

83. A thermodynamic process of uncontrolled change satisfying the equation Q = W = 0(zero) is known as [Q = heat supplied, W = work done]

a) Cyclic process b) Isothermal process c) Isochoric process d) Free expansion

84. Out of the following graphs, which p-V diagram represents isochoric process?





- 85. Which one of the following statement is NOT correct for an isochoric process?a) The volume remains b) The energy
 - constant. exchanged is used to change internal energy
 - c) The temperature of d) The work done is the system changes positive
- 86. An ideal gas at 27°C is compressed adiabatically to (8/27) of its original volume. If ratio of specific heats, $\gamma = 5/3$ then the rise in temperature of the gas is

a) 500 K	b) 125 K
c) 250 K	d)375 K

87. A monoatomic gas at pressure 'P' having volume 'V' expands isothermally to a volume 2V and then adiabatically to a volume 16V. The

final pressure of the gas is $\left(\gamma = \frac{5}{3}\right)$

a)
$$\frac{P}{64}$$
 b) $\frac{1}{1}$
c) $\frac{P}{8}$ d) $\frac{I}{3}$

88. In an adiabatic expansion of a gas initial and final temperatures are T_1 and T_2 respectively then the change in internal energy of the gas is $[R = gas constant, \gamma = adiabatic ratio]$

c)
$$\frac{R}{v-1}(T_2 - T_1)$$
 d) $\frac{R}{v-1}(T_1 - T_2)$

- 89. In an isochoric process, if $t_1 = 27^{\circ}C$ and $t_2 = 127^{\circ}C$, then $\frac{P_1}{P_2}$ will be equal to $[P_1$ and P_2 are the pressure at $t_1 0^{\circ}C$ and $t_2 ^{\circ}C$ respectively] a) 4/3 b) 9/59 c) 2/3 d) $\frac{3}{4}$
- 90. In an adiabatic process the state of a gas is changed from P_1 , V_1 , T_1 to P_2 , V_2 , T_2 out of the following relations, the correct one is

a)
$$P_1 V_1^{\gamma} = P_2 T_2^{\gamma}$$

b) $T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$
c) $P_1 V_1^{\gamma-1} = P_2 V_2^{\gamma-1}$
d) $T_1 V_1^{\gamma} = T_2 V_2^{\gamma}$

91. In the following p-V diagram, two adiabates cut two isothermals at T_1 and T_2 the value of v_b/v_c is



- a) Adiabatic b) Isobaric
 - c) Isothermal d) Isochoric
- 93. An ideal monoatomic gas is taken from A to B by the following three ways p, q, r as shown in the given p-V curve.



Then, amongst which of these ways, the internal energy would be same?

a) p and r

c) p and q

b) q and r d) For all the ways,

internal energy is same

94. One mole of an ideal diatomic gas undergoes a transition from A to B along a path AB as shown in the figure.



The change in internal energy of the gas during the transition is

a) 20 kJ	b) - 20 kJ
c) 20 J	d) - 12 kJ

95. Which one of the following equations specifies an isochoric process?

	$[Q = heat supplied, \Delta p \Delta V = change in volum temperatural$	e = change in pressure, e, $\Delta T = change in$	р	(3p, 3V)	(3p, 3V) B		
	contracting = 0	h $AD = 0$					
	$a)\Delta v = 0$	$d)\Delta P = 0$			¥		
96	$C_{J}Q = 0$ Three samples of the s	$a_{J}\Delta I = 0$					
90.	$(3)_1$	anie gas A, D anu C		D	$\Box_{C_{(n,3V)}}$		
	$\left(\gamma = \frac{1}{2}\right)$ have initially e	equal volume. Now		(p, V)	(p, 5 +)		
	volume of each sample	e is doubled. The process				→ V	
	is adiabatic for gas A, i	sobaric for B and	a)	pV	1	o)2pV	
	isothermal for C. If the	final pressures are	c)	4pV		d)zero	
	equal for all the three	samples, the ratio of	102.A	thermodyna	mic proce	ess of uncontrolle	ed
	their initial pressure is		ch to	lange satisfyi	ng the eq	uation $Q = W =$	0, 1S
	a) 2:1:2	b) $\sqrt{2}$: 1: $\sqrt{2}$		v = heat supp	d, W =	work donej	
	c) 2√2: 1: 2	d)2:1:√2	a)	Free expans.		d) Loothormol	
97.	During an adiabatic pr	ocess, the pressure p of	102 If	the heat of 1	10 Lic add	a) isourier mar	
	a fixed mass of an idea	I gas changes by Δp and	103.11	ute near of 1	internal	anorovis 40 L Th	non
	its volume V changes t	by ΔV . If $\gamma = C_p / C_v$, then	th	e amount of	external v	vork done is	icii,
	$\Delta v / v$ is given by	Λ n .	al	140 I	externar v	b) 70 I	
	a) $-\frac{p}{p}$	b) $-\gamma \frac{-r}{p} \Delta$	c)	1101	(d) 150 I	
	c) $\frac{\Delta p}{m}$	d) $\frac{\Delta p}{m^2 m}$	104.1	g of water of	volume 1	cm ³ at 100° c is	
98	Ideal gas for which 'y'	= 15 is suddenly	со	onverted into	steam at	same temperatu	re
,01	compressed to $1/4^{\text{th}}$ or	f its initial volume. The	ur	nder normal a	atmosphe	eric pressure (=	1×105
	ratio of the final press	ure to the initial	Pa	a). The volum	ie of stear	n formed equals	1671
	pressure is $\left(\gamma = \frac{C_P}{C_P} \right)$		cn	n ³ . If the spec	cific latent	t heat of vaporiza	ation
	(C_V)	h) 0.1	of	water is 225	6 J/g . the	e change in inter	nal
	a) 4:1 c) 1:16	d) 1:8	en	iergy is	1	-) 2000 I	
99	1 cm ³ of water at its h	niling point absorbs 540	a)	2423 J 167 J	I A	0J2089J	
,,,,	cal of heat to become s	steam with a volume =	105 Ar	107 J nongst the fo	ullowing r	elations which is	s true
	1671 cm ³ and the mec	hanical equivalent of	in	the case of a	n adiabat	ic process, wher	e =
	heat = 4.19 Jcal^{-1} at no	ormal pressure of 1.013	C _r	$/C_v$?			-
	\times 10 ⁵ Nm ⁻² . The energy	y spend in this process in	a)	$p^{1-\gamma}T^{\gamma} = co$	nstant l	b) $p^{\gamma}T^{1-\gamma} = cons$	stant
	overcoming intermole	cular forces is	c)	$pT^{\gamma} = const$	ant o	d) $p^{\gamma}T = constant$	ıt
	a) 540 cal	b)40 cal	106.Tł	ne pressure in	nside a ty	re is 4 atm at 27	°C. If
	c) 500 cal	d)zero	th	e tyre bursts	suddenly	, its final temper	ature
100	Which one of the follow	wing statements is	W	ill be (Here, γ	y = 7/5)		
	wrong for an isobaric	process?	a)	$300(4)^{7/2}$	1	$(4)^{2/7}$	
	a) The pressure of the	b) There is change in	c)	$300(2)^{7/2}$	(d) $300(4)^{-2/7}$	
	constant	is done	107.In	thermodyna	mic proc	esses which of th	ie
	c) Temperature of the	d) Energy exchanged is	fo	llowing state	ments is '	'NOT CORRECT')
	system remains	used to do work to	a)	In an isocho	ric	In an adiabatic	
	constant	change internal		process pres	ssure	$process, PV^{\circ} =$	
		energy		remains con	stant i	symbols have	e
101	An ideal monoatomic §.	gas is taken around the				meaning	
	cycle ABCDA as shown	n in following p – V	റ	In an isother	mal d	d)In an adiabatic	2
	diagram. The work do	ne during the cycle is		process. the		process, the sv	stem
				temperature)	is insulated fro	om
				remains con	stant	surroundings.	

108.An ideal gas at 27°C	is compressed
adiabatically to $\left(\frac{8}{27}\right)$) of its original volume. If
the ratio of specific	heats (γ) is $\left(\frac{5}{3}\right)$ then the
rise in temperature	of a gas is
a) 375 K	b) 125 K
c) 250 K	d) 500 K
109. The relation obeyed	l by a perfect gas during a
adiabatia pro assa ia	DV3/2 The initial

109. The relation obeyed by a perfect gas during an adiabatic process is $PV^{3/2}$. The initial temperature of the gas is 'T'. When the gas is compressed to half of its initial volume, the final temperature of the gas is a) $2\sqrt{2}T$ b) 4T

c) $\sqrt{2}$ T	d)2T
-----------------	------

110. Figure shows four p – V diagrams. Which of these curves represent isothermal and adiabatic process?



a) D and C	b) A and C
c) A and B	d) B and D

111. If ' Δ Q' is the amount of heat supplied to 'n' moles of a diatomic gas at constant pressure. ' Δ U' is the change in internal energy and ' Δ W' is the work done, then Δ W: Δ U: Δ Q is a) 1:2:3 b) 2:5:7

c) 2:3:4 d) 5:7:9

- 112. Which one of the following is NOT is true statement for an isothermal process?
 - a) Temperature of b) The process is very process remains fast constant
 - c) The equation of stated) There is no change in is PV = constant internal energy of the system
- 113.A sample of an ideal gas is taken through the cyclic process abca as shown in the figure. The change in the internal energy of the gas along the path ca is -180 J. The gas absorbs 250 J of heat along the path ab and 60 J along the path bc. The work done by the gas along the path abc is



N.B.Navale

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4.THERMODYNAMICS

						: ANS	W
1)	а	2)	b	3)	С	4)	b
5)	с	6)	d	7)	а	8)	С
9)	а	10)	b	11)	а	12)	d
13)	b	14)	b	15)	С	16)	d
17)	а	18)	d	19)	d	20)	а
21)	а	22)	b	23)	b	24)	d
25)	b	26)	С	27)	С	28)	а
29)	d	30)	а	31)	а	32)	а
33)	а	34)	а	35)	d	36)	С
37)	С	38)	d	39)	d	40)	d
41)	d	42)	d	43)	b	44)	а
45)	d	46)	b	47)	С	48)	С
49)	а	50)	b	51)	С	52)	С
53)	d	54)	b	55)	d	56)	а
57)	b	58)	С	59)	b	60)	d
61)	b	62)	С	63)	b	64)	b
65)	С	66)	b	67)	С	68)	а
69)	b	70)	d	71)	d	72)	b
73)	а	74)	а	75)	b	76)	b
77)	С	78)	b	79)	b	80)	b
81)	d	82)	d	83)	d	84)	а
85)	d	86)	d	87)	а	88)	С
89)	d	90)	b	91)	a	92)	а
93)	d	94)	b	95)	а	96)	С
97)	с	98)	b	99)	С	100)	С
101)	с	102)	a	103)	b	104)	b
105)	a	106)	d	107)	а	108)	а
109)	с	110)	а	111)	b	112)	b
113)	b	114)	a	115)	а	116)	d
117)	b	118)	b	,		,	
		110)	5				

N.B.Navale

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4.THERMODYNAMICS

: HINTS AND SOLUTIONS :

Single Correct Answer Type

1 **(a)**

Process 1 is isobaric (= constant) expansion. Hence, temperature of gas will increase. $\therefore \quad \Delta U_1 = \text{positive}$ Process 2 is an isothermal process

$$\therefore \Delta U_2 = 0$$

Process 3 is adiabatic expansion.

Hence, temperature of gas will fall.

 $\therefore \Delta U_3 = negative$

 $\therefore \Delta U_1 > \Delta U_2 > \Delta U_3$

2 **(b)**

In adiabatic process $\Delta Q=0,$ in isothermal process $\Delta U=0$ and in isochoric process W=0

3 **(c)**

AB and CD are isothermal curves, therefore $T_a = T_b$ and $T_c = T_d$ but all the four temperatures are not equal.

4 **(b)**

We know that, from first law of thermodynamics,

 $\Delta Q = \Delta U + \Delta W$

Work done at constant pressure,

 $(\Delta W)_{\rm p} = (\Delta Q)_{\rm p} - \Delta U$

As we know, $(\Delta Q)_V = \Delta U$

Also, $(\Delta Q)_p = nC_p\Delta T$

and $(\Delta Q)_V = nC_V \Delta T \Rightarrow (\Delta W)_p = n(C_p - C_V) \Delta T$

 $\Rightarrow (\Delta W)_{p} = 1 \times (3.4 \times 10^{3} - 2.4 \times 10^{3}) \times 10$

 $(\Delta W)_p = 10^4 \text{ cal}$

5 **(c)**

 $\frac{C_p}{C_w} = \frac{3}{2}$

Case I: Isothermal process

 $P_1 V_1 = P_2 V_2$ $PV = P_2 \times 9V$ $\therefore P_2 = \frac{P}{9}$

Case II: Adiabatic process

$$P_2 V_2^{\gamma} = P_3 V_3^{\gamma}$$
$$\frac{P}{9} (9V)^{\gamma} = P_3 (V)^{\gamma}$$
$$P_3 = \frac{P}{9} 9^{\gamma} \frac{V^{\gamma}}{V^{\gamma}} = \frac{P}{9} 9^{\frac{3}{2}}$$
$$= \frac{P}{9} \times 27 = 3P$$

6 **(d)**

Consider n moles of a gas which undergo isochoric process, i.e. V = constant. From first law of thermodynamics,

 $\Delta Q = \Delta W + \Delta U$

Here, $\Delta W = 0 \Rightarrow \Delta Q = \Delta V$...(i) As, we konw, $\Delta Q = nC_v\Delta T$ Substituting in Eq. (i), we get $\Delta U = nC_V\Delta T$...(ii) Mayer's relation can be written as $\Rightarrow C_p = C_v - R$

 $\Rightarrow C_v - C_p = R$...(iii)

From Eqs. (ii) and (iii), we have

$$\begin{split} \Delta U &= n(C_p - R) \Delta T \\ \text{Given, } n &= 6, C_p = 8 \text{ cal mol}^{-1} \text{ K}^{-1}, \\ R &= 8.31 \text{ J mol}^{-1} \text{ K}^{-1} = 2 \text{ cal mol}^{-1} \text{ K}^{-1} \\ \text{Hence, } \Delta U &= 6(8 - 2)(35 - 20) = 6 \times 6 \times 15 = 540 \text{ cal} \end{split}$$

(a) R. M. S. velocity $C \propto \sqrt{T}$

7

$$\therefore \frac{\mathsf{C}_2}{\mathsf{C}_1} = \sqrt{\frac{\mathsf{T}_2}{\mathsf{T}_1}} = \frac{1}{3}$$

$$\therefore \frac{\mathrm{T}_2}{\mathrm{T}_1} = \frac{1}{9}$$

For an adiabatic process

$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{\gamma - 1} = \frac{T_1}{T_2} = 9$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{\frac{3}{2} - 1} = 9$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{\frac{1}{2}} = 9$$
$$\therefore \frac{V_2}{V_1} = 81$$

8 (c)

Since, the volume of cylinder is fixed and helium is a monoatomic gas.

The internal energy $= nC_v \Delta T$ $U = \frac{1}{2} f n R \Delta T$

$$(:: \operatorname{cv} = \frac{1}{2} \operatorname{f} \operatorname{R})$$
$$U = \frac{1}{2} \times 3 \times 2 \times 8.31 \times 20$$

498 J

9 **(a)**

From first law of thermodynamics, $\Delta Q = \Delta U + \Delta W = \Delta U + p \Delta V$

 $\Rightarrow \qquad 100 = \Delta U + 50 - (4 - 10) \Rightarrow \Delta U = 400 \text{ J}$

10 **(b)**

According to the question, Heat spent during the conversion of sample of water at 100°C to steam is

$$\Delta Q = 54 \text{ cal} = 54 \times 4.18 \text{ J}$$

=225.72 J

Normal pressure ,p = 1.1013×10^5 Nm⁻² Net work done during the conversion would be given as $\Delta W = p \Delta V$

 $= p[V_{steam} - V_{water}]$ Here, $V_{steam} = 167.1 \text{ cc} = 167.1 \times 10^{-6} \text{ m}^3$ $V_{water} = 0.1 \text{ g} = 0.1 \text{ cc} = 0.1 \times 10^{-6} \text{ m}^3$ $\therefore \quad \Delta W = 1.013 \times 10^5 [(167.1 - 0.1) \times 10^{-6}]$ $= 1.013 \times 167 \times 10^{-1} = 16.917 \text{ J}$

Now, from first law of thermodynamics, $\Delta Q = \Delta U + \Delta W$

where, ΔU is the change in internal energy of the sample.

 $\Delta U = \Delta Q - \Delta W$

Substituting the values in the above equation, we get

$$\Delta U = 225.72 - 16.917 = 208.8 \text{ J}$$

11 **(a)**

 \Rightarrow

For isothermal process, pV = constant.

Therefore, p - V graph is a rectangular hyperbola. Since, $T_2 > T_1$

$$\Rightarrow \quad (pV)_{at} T_2 > (pV)_{at} T_1$$

 \Rightarrow Thus, the graph given in option (a) correctly represents the given situation.

12 **(d)**

Since density becomes twice, its volume will become half.

$$\div \frac{V_1}{V_2} = 2$$

 \therefore For adiabatic process we have

$$\therefore P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$
$$\therefore \frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^{\gamma} = (2)^{7/5} = (2)^{1.4} = 2.63$$

13 **(b)**

For isothermal expansion we have

$$P_1V_1 = P_2V_2$$

 $\therefore P_2 = P_1\frac{V_1}{V_2} = P_1 \times \frac{1}{2} = \frac{P_1}{2}$

For adiabatic process:

 $\therefore P_1 = \frac{1}{2}$

14

$$P_{1}V_{1}^{\gamma} = P_{2}V_{2}^{\gamma}$$

$$\therefore P_{2} = P_{1}\left(\frac{V_{1}}{V_{2}}\right)^{\gamma} = P_{1}\left(\frac{1}{2}\right)^{\gamma} = \frac{P}{2^{\gamma}}$$

$$\therefore P_{a} = \frac{P}{2^{\gamma}}$$

$$\therefore \frac{P_{i}}{P_{a}} = \frac{2^{\gamma}}{2} = 2^{\gamma-1}$$
(b)
$$T_{1} = 27^{\circ}C = 27 + 273 = 300 \text{ K}$$

$$V_1 = V, V_2 = \frac{V}{8}, \gamma = \frac{5}{3}$$

For an adiabatic process $TV^{\gamma-1} = constant$

$$\therefore T_1 V^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$

$$\therefore \frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma - 1} = (8)^{\frac{5}{3} - 1} = (8)^{\frac{2}{3}} = 4$$

$$\therefore T_2 = 4T_1 = 4 \times 300 = 1200 \text{ K}$$

16 **(d)**

υ τηλ

For adiabatic expression, we have

$$P_{2}V_{2}^{\prime} = P_{1}V_{1}^{\prime}$$
$$\therefore \frac{P_{2}}{P_{1}} = \left(\frac{V_{1}}{V_{2}}\right)^{\gamma} = (8)^{\frac{4}{3}} = 16$$

$$\therefore P_2 = 16P_1 = 16P_0$$

D 17

17 **(a)**

In isochoric process, volume remains constant and hence no work is done. Hence statements (A) is incorrect.

18 **(d)**

The internal energy of a gas contained in a movable box depends only on the molecular energies.i.e.it is the sum of the kinetic energies and potential energies of the molecules of gas. The kinetic energy of the moving box is not included in the internal energy, thus internal energy does not depend on the speed v of the box

19 **(d)**

Here, dQ = 400 cal, dW = -105 J = -(105/4.2) cal = -25 cal, dU = ?Now, dU = dQ - dW = 400 - (-25) = 425 cal Note dW is negative because work is done on the system.

20 **(a)**

When a system undergoes a change under condition that no exchange of heat takes place between the system and surroundings, then such a process is called adiabatic.

$P^{1-y}T^y = constant$

Where , is ratio of specific heats, p is pressure and T is temperature.

÷

 \Rightarrow

....

$$\left(\frac{\mathrm{p2}}{\mathrm{p1}}\right)^{\gamma-1} = \left(\frac{T_2}{T_1}\right)^{\gamma}$$

$$\left(\frac{1}{2}\right)^{0.4} = \left(\frac{T_2}{300}\right)^{1.4}$$

$$\left(\frac{1}{2}\right)^{\frac{2}{\gamma}} = \left(\frac{T_2}{300}\right) \Rightarrow \mathrm{T}_2$$

21 (a)
R. M. S. velocity

$$C \propto \sqrt{T}$$

 $\therefore \frac{C_2}{C_1} = \sqrt{\frac{T_2}{T_1}}$
 $\therefore \frac{1}{2} = \sqrt{\frac{T_2}{T_1}}$
 $\therefore \frac{T_2}{T_1} = \frac{1}{4}$

For adiabatic process

4

$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{\gamma - 1} = \frac{T_1}{T_2} =$$
$$\left(\frac{V_2}{V_1}\right)^{1.5 - 1} = 4$$
$$\left(\frac{V_2}{V_1}\right)^{\frac{1}{2}} = 4$$
$$\therefore \frac{V_2}{V_1} = 16$$

22 **(b)**

23

 $= 246.1 \, \text{K}$

For adiabatic expansion, we have the formula $pV^{\gamma} = constant$...(i) Gas equation, $pV = RT \Rightarrow p = \frac{RT}{V}$ (ii) From Eqs. (i) and (ii), we obtain $\left(\frac{\text{RT}}{\text{V}}\right)$ V^{γ} = constant \Rightarrow TV^{γ -1} = constant (iii) $T \propto \frac{1}{\sqrt{V}}$ (given) But \Rightarrow TV^{1/2}= constant (iv) Thus, using Eqs. (iii) and (iv), we get $\gamma - 1 = \frac{1}{2}$ $0r \gamma = \frac{3}{2} = 1.5$ $\Rightarrow \frac{C_p}{C_w} = 1.5$ (b) R. M. S. velocity $C \propto \sqrt{T}$

$$\therefore \frac{C_2}{C_1} = \sqrt{\frac{T_2}{T_1}}$$
$$\therefore \frac{1}{2} = \sqrt{\frac{T_2}{T_1}}$$
$$\therefore \frac{T_2}{T_1} = \frac{1}{4}$$

For adiabatic expansion,

4

$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{\gamma - 1} = \frac{T_1}{T_2} =$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{1.5 - 1} = 4$$
$$\therefore \left(\frac{V_2}{V_1}\right)^{0.5} = 4$$
$$\therefore \frac{V_2}{V_1} = 16$$

24 (d)

 $dW = dQ - dU = C_p (T_2 - T_1) - C_v (T_2 - T_1)$ $= R (T_2 - T_1)$ $= 8.31 \times 100$ $= 8.31 \times 10^{-2}$ J

25 (b)

For an adiabatic process $TV^{\gamma-1} = constant$

30

$$\gamma = \frac{7}{5}$$

$$\therefore \gamma - 1 = \frac{7}{5} - 1 =$$

$$\therefore TV^{\frac{2}{5}} = TV^{x}$$

$$\therefore x = \frac{2}{5}$$

26 (C)

In thermodynamics, heat and work are not state variables. They are modes of energy transfer to a system resulting in change in its internal energy, which is a state variable.

27 (c)

According to the first law of thermodynamics, Heat supplied $(\Delta Q) = Work done (W) + Change$ in internal energy of the system (ΔU)

 $\Delta Q_A = \Delta U_A + W_A.$ Similarly, for process B, $\Delta Q_{\rm B} = \Delta U_{\rm B} + W_{\rm B}$ Now, we know that, work done for a process = area under its p - Vcurve Here, р \cap Vf V Thus, it is clear from the above graphs, $W_A > W_B$...(i) Also, since the initial and final state are same in both process, so $\Delta U_A = \Delta U_B$...(ii) So, from Eqs. (i) and (ii), we can conclude that $\Delta Q_A > \Delta Q_B$ 29 (d) Heat and work are two distinct modes of energy transfer to a system that results in change in its internal energy. Thus either by extracting heat or doing work On the system or if work is done by system on surrounding, the internal energy of the system can be changed. (a) In an adiabatic process, $pV^{\gamma} = constant = k (say)$ where, p is pressure, V is volume and γ is ratio of the specific heats. Given, $\frac{C_p}{C_V} = \gamma = \frac{3}{2}$ $\therefore pV^{3/2} = k$ Taking logarithm of both sides, we get

$$\log p + \frac{3}{2} \log V = \log k$$

$$\therefore \frac{\Delta p}{p} + \frac{3}{2} \frac{\Delta V}{V} = 0$$

$$\Rightarrow \frac{\Delta V}{V} = -\frac{2}{3} \frac{\Delta p}{p}$$

$$\Rightarrow \frac{\Delta V}{V} \times 100 = -\frac{2}{3} \left(\frac{\Delta p}{p} \times 100\right) = -\frac{2}{3} \times \frac{2}{3} = -\frac{4}{9}\%$$

Negative sign implies that volume decreases by $\frac{4}{9}$ %.

31 **(a)**

If the graph is parallel to pressure axis, the volume is constant.

 $W = P\Delta V$

Since, $\Delta V = 0$, W = 0

32 **(a)**

Amount of sweat evaporated/minute Sweat produced / minute

_	
	Number of cals required for evaporation / kg
_	$14.5 imes 10^4$
	580×10^3

 $=\frac{145}{580}=0.25$ kg

33 **(a)**

 $\frac{V_2}{V_1} \!=\! \frac{1}{8}, \gamma = \! \frac{5}{3}$

For adiabatic process,

$$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

 $\therefore \frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^{\gamma} = (8)^{5/3} = (2)^5 = 32$

34 **(a)**

An isothermal process is a constant temperature process. In this process

 $T = constant \text{ or } \Delta T = 0$

 $\therefore \quad \Delta U = nC_V \Delta T = 0$ An adiabatic process is defined as one with no heat transfer into or out of a system. Therefore $\Omega = 0$ From the first law of

Therefore, Q = 0. From the first law of thermodynamics, $W = -\Delta U$ or $\Delta U = -W$

35 **(d)**

By first law of thermodynamics

 $\Delta Q = \Delta U + W$

For an adiabatic process $\Delta Q = 0$

 $\therefore \Delta U = -W$

36 **(c)**

37 (c)

As, it is known, $\frac{\text{slope of adiabatic curve}}{\text{slope of isothernmal curve}} = \frac{\gamma p/V}{p/V} = \gamma = \frac{Cp}{Cv}$ According to the question $V = kT^{2/3}$ $\therefore dV = k\frac{2}{3}T^{-1/3}dT$ (after differentiating) $dV = kT^{-1/3}dT = 2 dT$

$$\therefore \frac{dV}{V} = \frac{3}{kT^{2/3}} = \frac{2}{3}\frac{dT}{T}$$

W ork done, $W = \int_{T_1}^{T_2} RT \frac{dV}{V} = \int_{T_1}^{T_2} RT \frac{2}{3}\frac{dT}{T}$
 $W = \frac{2}{3}R(T_2 - T_1) = \frac{2}{3}R \times 60 = 40R$

38 **(d)**

As indicator diagrams in all the three cases are closed curves, representing cyclic changes, therefore U = constant and $\Delta U = 0$ in all the cases.

39 **(d)**

In isochoric process, the volume remains constant and hence work done dw = P. dv in zero.

40 **(d)**

In isobaric process pressure remains constant

41 **(d)**

Given, n = 10 mol, T = 500 K, $V_1 = 50 L$ and $V_2 = 5 L$ Work done at constant temperature (i.e. isothermal process), $W_1 = 2.2 n PT \log {\binom{V_2}{2}}$

$$W = 2.3 \text{ nR I } \log_{10}\left(\frac{1}{V_1}\right)$$
$$= 2.3 \times 10 \times 8.31 \times 500 \times \log_{10}\left(\frac{5}{50}\right)$$

$$= -9.5565 \times 10^4 \text{ J}$$

$$\approx -9.6 \times 10^4$$
 J

42 **(d)**

For isothermal process $Q \neq 0$

43 **(b)**

Area under the curve is maximum in isobaric process.

44 **(a)**

In a cyclic process, work done is equal to area of the loop ACBDA representing the cycle of changes.

45 **(d)**

In isothermal process, temperature remains constant.

 $\therefore \Delta U = 0$

In isochoric process, volume remains constant, work done is zero, hence $\mathbf{Q}=\Delta U$

In adiabatic process, Q=0 hence $\Delta U=-w$

In isobaric process Δw ≠ 0, hence ΔU ≠ 0
46 (b) As work done in a process = area under the curve. As the area under the curve is increasing with time; so, the work done is also increases continuously.
47 (c) Isobaric expansion is represented by curve AB. Work done = Area under AB = 2 × 10² × (3 - 1)

 $= 4 \times 10^2 = 400$ J

48 (c)

In adiabatic process, heat remains constant. So, from first law of thermodynamics,

 $\Delta Q = \Delta U + \Delta W$ $\Rightarrow \quad \Delta U + \Delta W = 0$ When work is done on system, $\Delta W = -ve$ $\Rightarrow \quad \Delta U = -\Delta W = +ve$ As, $\Delta U = nC_V \Delta T = +ve \Rightarrow \Delta T = +ve$

$$\Rightarrow$$
 T increases or T_f > T_i.

49 **(a)**

As, $W_{CB} = p\Delta V = nR\Delta T = -nR(2T_0 - T_0) =$ $-nRT_0$ $W_{BA} = p\Delta V = 0$ (:: $\Delta V = 0$) and $W_{AC} = nRTln\left(\frac{V_2}{V_1}\right) = 2nRT_0ln\left(\frac{2V_0}{V_0}\right)$ $= +2nRT_0ln 2$ Total work done $= W_{AC} + W_{CB} + W_{BA}$ $= 2 nRT_0ln 2 - nRT_0 + 0$ $= nRT_0(2ln 2 - 1)$ Also, input heat, $\Delta Q_{BC} = nC_p\Delta T = \frac{nR\gamma T_0}{\gamma - 1}$ \therefore Efficiency $= \frac{W \text{ ork done}}{ln \text{ put heat}} = \frac{(2ln 2 - 1)}{\gamma/(\gamma - 1)}$

50 **(b)**

Work done during the process AB is given by area under the line AB

$$W = P(v_2 - v_1)$$

= 4 × 10² × (6 - 2)
= 16 × 10² J
= 1600 J

51 **(c)**

For the given system, Volume (V) = (l) (A) Let piston moves a distance dl. \Rightarrow dV = A dl, for constant A ...(i) Force on piston = (pressure) (area) =pA

So, work = force distance = (p A) (dl) = p (A dl)dW = p dV[using Eq.(i)] $\Rightarrow \Delta W = p \Delta V$ 52 (c) In isothermal expansion, $V_2 > V_1$ As, work done in an isothermal process is given bv $\Delta W = nRT \ln \frac{V_2}{V}$ \Rightarrow In this case, $\Delta W_1 > 0$ $\Delta W_1 = + ve$ or Similarly, in isothermal compression, $V_1 > V_2$ $\Rightarrow \Delta W_2 < 0$ $\Rightarrow \Delta W_2 = -ve$ 53 (d) For adiabatic process, $pV^{\gamma} = TV^{\gamma-1} = constant$ $\Rightarrow \frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma - 1}$ Here, $T_2 = 2T_1$ and $V_2 = \frac{V_1}{2}$ $\left(\frac{1}{2}\right)^{\gamma-1} = \left(\frac{1}{2}\right)$ $\Rightarrow \gamma - 1 = 1 \text{ or } \gamma = 2$ $\Rightarrow pV^{\gamma} = pV^2 = constant$ 54 **(b)** For an adiabatic process $PV^{\gamma} = constant$. $\therefore P_1 V_1^{\gamma} = P_2 V^{\gamma}$ $\therefore \frac{P_2}{P_4} = \left(\frac{V_1}{V_2}\right)^{\gamma} = (8)^{4/3} = 16$ $\therefore P_2 = 16P_1 = 16P_0$ 55 (d) For an adiabatic process, $T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$ or $T_1 L_1^{\gamma - 1} = T_2 L_2^{\gamma - 1}$ (:: A = Constant)or $\frac{T_1}{T_2} = \left(\frac{L_2}{L_1}\right)^{\gamma-1}$ $\therefore \gamma = \frac{5}{2}$ for a monoatomic gas, $\therefore \gamma - 1 = \frac{2}{3}$ Thus, $\frac{T_1}{T_2} = \left(\frac{L_2}{L_2}\right)^{2/3}$ 56 (a) Initial and final states are same in all the process. Hence, $\Delta U = 0$ is same for each case. $\Delta Q = \Delta U + \Delta W = \Delta W$ = Area enclosed by curve with volume axis. \therefore (Area)₁ < (Area)₂ < (Area)₃

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 $\Rightarrow Q_1 < Q_2 < Q_3$

57 **(b)**

For an adiabatic process at constant pressure we have

TV^{γ-1} = constant ...(1)
Given
T ∝
$$\frac{1}{\sqrt{V}}$$

∴ TV^{1/2} = constant
By (1) and (2)

 $\gamma - 1 = \frac{1}{2}$ $\therefore \gamma = 1.5$

58 **(c)**

When the cylinder is put in contact with a body at a higher temperature than that of gas, then the temperature difference will cause a flow of energy (heat) from hotter body to gas. This increase the internal energy of the gas.

Similarly, if we push the piston down, i.e. do some work on the system, it also results in increasing the internal energy of the gas.

Thus internal energy or state of the gas can be changed by either of the ways mentioned in options (a) and (b).

59 **(b)**

We have

 $\Delta Q = \Delta U + \Delta W$

In an adiabatic process, $\Delta 0=0$

 $\therefore \Delta U = -\Delta W$

60 **(d)**

According to the first law of thermodynamics

 $\Delta Q = \Delta U + \Delta W$

If $\Delta W = 0$, then $\Delta Q = \Delta U$

If $\Delta Q < Q$, then $\Delta U < 0$

If internal energy decreases, then temperature will decrease.

61 **(b)**

In a thermodynamic system, working substance is an ideal gas. Its internal energy is in the form of only kinetic energy.

62 **(c)**

Extensive state variables indicate the size of the system, whereas intensive do not.

So, if the system in equilibrium is divided into two equal parts, the variables that remain unchanged for each part are intensive. On contrary, the variables whose value get halved in each part are extensive.

So, from the given values, we can say that U (internal energy) and M (mass) are extensive state variables and T (temperature) is an intensive state variable.

63 **(b)**

Since the system is isolated from the surroundings, it is an adiabatic process. Since the gas expands into vacuum the external pressure is zero and hence work done is zero. There will be no change in internal energy and hence no change in temperature.

64 **(b)**

For adiabatic process

$$W = \frac{nR(T_2 - T_1)}{1 - \gamma}$$

$$W = -125 \text{ kJ, n} = 1 \text{ kmole,}$$

$$T_2 - T_1 = 6^{\circ}C$$

$$\therefore 1 - \gamma = \frac{nR(T_2 - T_1)}{W} = \frac{1 \times 8.3 \times 6}{-125} = -0.4$$

$$\therefore \gamma = 1.4$$

∴ Gas is rigid diatomic.

65 **(c)**

For adiabatic process $PV^{\gamma}=constant$ and PV=nRT

 $\therefore PT^{\gamma-1} = constant$

BC is adiabatic, $T_1 V_b^{\gamma-1} = T_2 V_c^{\gamma-1} \ \ ... (i)$

AD is adiabatic,
$$T_1 V_a^{\gamma-1} = T_2 V_d^{\gamma-1}$$
 ... (ii)

So,
$$\left(\frac{V_{b}}{V_{a}}\right)^{\gamma-1} = \left(\frac{V_{c}}{V_{d}}\right)^{\gamma-1}$$

$$\therefore \frac{V_{\rm b}}{V_{\rm a}} = \frac{V_{\rm c}}{V_{\rm d}}$$

67

(c) For adiabatic process, $p_2 V_2^{\gamma} = p_1 v_1^{\gamma}$ \therefore Final pressure, $p_2 = p_1 \left(\frac{V_1}{V_2}\right)^{\gamma} = p_1 \left(\frac{p_2}{p_1}\right)^{\gamma}$

For an adiabatic process

$$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^{\gamma}$$

$$\frac{V_1}{V_2} = 4$$

$$= (4)^{\frac{5}{2}} = 2^5 = 32$$

$$\therefore P_2 = 32P_1 = 32P$$

69 **(b)**

In isobaric process, pressure remains constant

 $= p \left(\frac{2}{1}\right)^{7/5} = 2.63 p$

70 (d)

According to the first law of thermodynamics

 $\Delta Q = \Delta U + \Delta W$

For adiabatic process

 $\Delta Q = 0$

 $\therefore \Delta U = -W$

71 (d)

 $\Delta Q = \Delta U + W$

 $68 = \Delta U + 30$

 $\therefore \Delta U = 68 - 30 = 38 \text{ K}$

72 **(b)**

For adiabatic expansion we have

$$T_1 V_1^{\gamma} = T_2 V_2^{\gamma - 1}$$
$$\therefore \frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma - 1} = \left(\frac{L_1}{L_2}\right)^{\gamma - 1} \quad [\because v \propto L]$$
$$= \left(\frac{L_1}{L_2}\right)^{\frac{5}{3} - 1} = \left(\frac{L_1}{L_2}\right)^{\frac{2}{3}}$$
$$[-5]$$

 $\left[\text{For monoatomic gas } \gamma = \frac{3}{3} \right]$

73 **(a)** PV = nRT

$$n = \frac{m}{M} = \frac{2}{32} = \frac{1}{16}$$

74 **(a)**

In isothermal process, temperature is constant. From ideal gas equation, pV = nRTAt constant temperature, pV = constant. So, with decreasing pressure p, V must increase to keep product pV constant. This inverse relation between p and V is depicted correctly by curve A, where p decreases with increasing V.

75 **(b)**

Here , n = 5 , $\gamma = \frac{7}{5}$, $T_1 = 0^{\circ}$ C, $T_2 = 400^{\circ}$ C

 \therefore The internal energy of gas , $dU = n \frac{nRdt}{(\gamma-1)}$

$$= \frac{5 \times 8.31 \times (400-0)}{\binom{7}{5}-1}$$

= 41550 J = 41.55 kJ

76 **(b)**

Area under the curve in P-V graph is maximum for isobaric process. Hence work done in maximum is isobaric process.

77 **(c)**

Given, dQ = +200 cal $= 200 \times 4.2 = 840$ J And dW = +40 J From first law of thermodynamics, dQ = dU + dW dU = dQ - dW = 840-40 = 800 J So, the internal energy of the system increases by 800 J.

78 **(b)**

In isothermal process, temperature of the gas remains constant, so the gas obeys Boyle's law. i.e.

$$p \propto \frac{1}{V} \Rightarrow \frac{p_2}{p_1} = \frac{V_1}{V_2}$$

$$\frac{2p}{p} = \frac{V_1}{V_2} \Rightarrow \frac{V_1}{V_2} = 2 \quad ...(i)$$
Now, the gas is expanded adiabatically, so
$$pV^{\gamma} = \text{ constant}$$

$$\frac{p_1}{p_2} = \left(\frac{V_2}{V_1}\right)^{\gamma}$$

$$\Rightarrow \frac{2p}{0.75p} = \left(\frac{2}{1}\right)^{\gamma} \quad (\text{since, volume is restored})$$

$$\Rightarrow \log\left(\frac{1}{3}\right) = \gamma \log 2$$
$$\log 8 - \log 3 = \gamma \log 2$$
$$\Rightarrow \gamma = 1.41$$

79 **(b)**

Efficiency
$$\eta = \frac{W}{Q_1} = \frac{Q_1 - Q_2}{Q_1} = \frac{T_1 - T_2}{T_1}$$

= $\frac{t_1 - t_2}{t_1 + 273}$

80 **(b)**

In cyclic process, ΔQ = work done = area inside the closed curve (treat the circle as an ellipse)

$$= \pi \frac{(p_2 - p_1)}{2} \frac{(V_2 - V_1)}{2}$$

$$\Rightarrow \Delta Q = \frac{\pi}{4} \{ (150 - 50) \times 10^3 \times (40 - 20) \times 10^{-6} \} = \left(\frac{\pi}{2}\right) J$$

81 (d)

According to question, $p \propto T^3$ As, $pV = nRT \Rightarrow T \propto pV$ $\Rightarrow p \propto (pV)^3 \Rightarrow p^2V^3 = constant$ $pV^{3/2} = constant$ $\therefore \frac{C_p}{C_v} = \gamma = \frac{3}{2}$ (:: $pV^{\gamma} = constant$)

82 **(d)**

 $T_1 = 27^{\circ}C = 27 + 273 = 300 \text{ K}$

$$\frac{V_2}{V_1} = \frac{8}{27}$$

$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$

$$\therefore T_2 = T_1 \left(\frac{V_2}{V_1}\right)^{\gamma - 1}$$

$$= 300 \times \left(\frac{27}{8}\right)^{\frac{5}{3} - 1}$$

$$= 300 \times \left(\frac{27}{8}\right)^{\frac{2}{3}}$$

$$= 300 \times \left(\frac{3}{2}\right)^2$$

Rise in temperature

83 (d)

A thermodynamic process of uncontrolled change satisfying the equation Q = W = 0 (zero) is known as free expansion.

84 **(a)**

In isochoric process volume remains constant.

Hence graph A represents isochoric process.

- 85 **(d)** For isochoric process, the work done is zero.
- 86 **(d)** For an adiabatic process $TV^{\gamma-1} = constant$

$$\begin{array}{l} \therefore \frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma-1} \\ = \left(\frac{27}{8}\right)^{\frac{5}{3}-1} = \left(\frac{27}{8}\right)^{\frac{2}{3}} = \frac{9}{4} \\ \therefore T_2 = \frac{4}{9} \cdot T_1 \\ = \frac{4}{9} \times 300 = 675 \text{ K} \\ \therefore T_2 - T_1 = 675 - 300 = 375 \text{ K} \\ \end{array} \\ \begin{array}{l} 87 \quad \textbf{(a)} \\ \text{For isothermal process:} \\ P_1 V_1 = P_2 V_2 \\ \therefore P_2 = \frac{P_1 V_1}{V_2} = \frac{P_1}{2} \\ \left(\because \frac{V_1}{V_2} = \frac{1}{2}\right) \\ \text{For adiabatic process:} \\ P_2 V_2^{\gamma} = P_3 V_3^{\gamma} \\ P_3 = P_2 \left(\frac{V_2}{V_3}\right)^{\gamma} \\ = P_2 \left(\frac{2V_1}{V_3}\right)^{\gamma} \\ = \frac{P_1}{2} \left(\frac{1}{8}\right)^{\frac{5}{3}} \\ \left[\because \frac{V_1}{V_3} = \frac{1}{16}\right] \\ = \frac{P_1}{2} \cdot \frac{1}{32} = \frac{P_1}{64} \end{array}$$

88 **(c)**

In adiabatic process work done is equal to the change in internal energy.

$$W = \frac{R}{\gamma - 1} (T_2 - T_1)$$

89 (d) $t_1 = 27^{\circ}C = 27 + 273 = 300 \text{ K}$

$$t_2 = 127^{\circ}C = 127 + 273 = 400 \text{ K}$$

In an isochoric process, volume remains constant.

$$\therefore \frac{P_1}{P_2} = \frac{t_1}{t_2} = \frac{300}{400} = \frac{3}{4}$$

90 **(b)** $P V^{\gamma} - P V^{\gamma}$

$$\frac{RT_{1}}{v_{1}} V_{1}^{\gamma} = \frac{RT_{2}}{V_{2}} V_{2}^{\gamma}$$

$$\frac{RT_{1}}{v_{1}} V_{1}^{\gamma} = \frac{RT_{2}}{V_{2}} V_{2}^{\gamma}$$

$\therefore \mathbf{T}_1 \mathbf{V}_1^{\gamma - 1} = \mathbf{T}_2 \mathbf{V}_2^{\gamma - 1}$

91 (a)

From symmetry considerations and also from theory,

 $\frac{v_a}{v_d} = \frac{v_b}{v_c}$

92 (a)

In adiabatic thermodynamic process, there is no exchange of heat between the system and surroundings.

93 **(d)**

Internal energy is a state variable which depends only on the state of the system, not on how that state was achieved. Thus, in the given case, internal energy of the ideal monoatomic gas would be same in all three ways taken by it to go from A to B.

94 **(b)**

For a diatomic gas, $C_v = \frac{5}{2}R$

The change in internal energy of gas in the transition from A to B.

$$\Delta U = nC_{v}dT$$

$$= \frac{5}{2}R\left(\frac{P_{B}V_{B}}{R} - \frac{P_{A}V_{A}}{R}\right) \qquad (:T = \frac{pV}{R})$$

$$= \frac{5}{2} \times (12 - 20) = -20kJ$$

95 (a)

In an isochoric process, the volume remains constant.

 $\therefore \Delta V = 0$

96 (c)

Given: $V_2 = 2V_1$, $\gamma = \frac{3}{2}$

For adiabatic process (gas A) :

$$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

$$\therefore \frac{P_1}{P_2} = \left(\frac{V_2}{V_1}\right)^{\gamma} = (2)^{\frac{3}{2}} = 2\sqrt{2}$$

 $P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$

 $\therefore P_1 = 2\sqrt{2}P_2$

For isobaric process (gas B) : In isobaric process pressure remains constant

$$\therefore P_1 = P_2 \text{ or } \frac{P_1}{P_2} = 1$$

For isothermal process (gas C) : In isothermal process, temperature remains constant.

:.
$$P_1 v_1 = P_2 v_2$$

or $\frac{P_1}{P_2} = \frac{v_2}{v_1} = 2$ or $P_1 = 2P_2$

∴ Ratio of initial pressure is $2\sqrt{2}$: 1: 2

97 (c)

As, B
$$\gamma p = -\frac{\Delta p}{\Delta V/V}$$

 $\therefore \quad \frac{\Delta V}{V} = -\frac{\Delta p}{\gamma p}$

98 **(b)**

For adiabatic process

$$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

$$\therefore \frac{P_2}{P_1} = (V_1/V_2)^{\gamma} = (4)^{3/2} = 8$$

As , from the first law of thermodynamics, dU = dQ - dW = m L - p (dV) $= 1 \times 540 - \frac{1.013 \times 10^{5} (1671 - 1)10^{-6}}{4.2}$ = 540 - 40 = 500 cal101 (c)

Work done = Area of curve enclosed
=
$$(3V - V) \times (3p - p) = 2V \times 2p = 4pV$$

102 (a)

A thermodynamic process of uncontrolled change satisfying the equation Q = W = 0, is free expansion.

103 **(b)**

Quantity of heat supplied to system is equal to increase in internal energy and external work. According to first law of thermodynamics, when some quantity of heat (dQ) is supplied to a system capable of doing external work, then the quantity of heat absorbed by the system (dQ) is equal to sum of the increase in the internal energy of the system (dU) due to rise in temperature and the external work done by the system (dW) in expansion, i.e.

dQ = dU + dW

When a gas expands, work done by the gas dW is taken as positive and when a gas is compressed, work is done on the gas dW is taken as negative. The external work done is

 $\Delta W = \Delta Q - \Delta U$

= 110 - 40 = 70 J

104 **(b)**

Given, mass of water m = 1gVolume of 1g of water = $1 \text{ cm}^3 = 10^{-6} \text{ m}^3$ Volume of 1 g of steam = $1671 \text{ cm}^3 = 1671 \times 10^{-6}$ m³ Pressure, $P = 1 \times 10^5$ pa Latent heat of vaporization of water, L = 2256 J/gChange in volume, $\Delta V = (1671-1) \times 10^{m3}$ $= 1670 \times 10^{-6} \,\mathrm{M}^{3}$...(i) Heat supplied, $\Delta Q = mL = 1 \times 2256 = 2256$ J ...(ii) As the steam expands, so the work done in expansion is $\Delta W = p\Delta V$ $= 1 \times 10^5 \times 1670 \times 10^{-6}$ [from Eq. (i)] =167 J ...(iii) According to first law of thermodynamics, $\Delta Q = \Delta U + \Delta W$ $\Rightarrow \Delta U = \Delta 0 - \Delta W$ = 2256 - 167[from Eqs. (ii) and (iii)] = 2089 J 105 (a) For adiabatic change, the equation of state is $pV^{\gamma} = constant$ Also, for ideal gas, pV = nRT $\Rightarrow V = \frac{nRT}{p}$

So, $p\left(\frac{nRT}{p}\right)^{\gamma} = \text{ constant}$

$$\Rightarrow \frac{p}{p^{\gamma}} T^{\gamma} = \frac{\text{constant}}{(nR)^{\gamma}} = \text{ constant}$$
$$\Rightarrow p_*^{1-\gamma} T^{\gamma} = \text{ constant}$$

106 **(d)**

In an adiabatic process, $p_2^{(1-\gamma)}T_2^{\gamma} = p_1^{(1-\gamma)}T_1^{\gamma}$ Final temperature, $T_2 = T_1 \left(\frac{p_1}{p_2}\right)^{(1-\gamma)/\gamma}$

$$= 300 \left(\frac{4}{1}\right)^{\frac{(1-7/5)}{7/5}}$$
$$= 300(4)^{-2/7}$$

108 **(a)**

For adiabatic process,

$$\therefore T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$

$$\therefore \frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma - 1} = \left(\frac{27}{8}\right)^{\frac{5}{3} - 1}$$

$$= \left(\frac{27}{8}\right)^{\frac{2}{3}} = \left(\frac{3}{2}\right)^2 = \frac{9}{4}$$

$$\therefore T_2 = \frac{9}{4} T_1 = \frac{9}{4} \times 300 = 675 \text{ K}$$

$$\therefore T_2 - T_1 = 675 - 300 = 375 \text{ K}$$

109 (c)

Relation between P and V is given as

$$PV^{\frac{3}{2}} = constant$$

 $\therefore \gamma = \frac{3}{2}$

The relation between T and V is given by

110 **(a)**

In curves A and B, pressure and volume both increase. Therefore, temperature must rise and heat must be supplied to do work. So, A and B cannot be required curves. Out of C and D, slope of D smaller. Therefore, D is isothermal curve and C is adiabatic curve.

111 (b)

We know,

 $\Delta Q = nC_{p}\Delta T$

 $\Delta U = nC_v \Delta T$

 $W = P\Delta V = nR\Delta T$

 $\Delta W: \Delta U: \Delta Q = R: C_v: C_p$

For a diatomic gas

f = 5

$$\therefore C_v = \frac{f}{2}R = \frac{5}{2}R$$

 $C_p - C_v + R = \frac{7}{2}R$
 $\therefore R: C_v: C_p = 1:\frac{5}{2}:\frac{7}{2} = 2:5:7$

112 (b)

In isothermal process, the temperature remains constant due to exchange of heat with the surroundings, which takes some time. Hence process is not very fast.

113 **(b)**

In Process $a \rightarrow b$ $\Delta Q_{ab} = 250 \text{ J}$ Given, $250 = \Delta U_{ab} + \Delta W_{ab}$:. (i) In Process $b \rightarrow c$ $\Delta Q_{bc} = 60 J$ Given, Also, V is constant, so $\Delta V = 0$ $\Delta W_{\rm bc} = p(\Delta V)_{\rm bc} = 0$ ⇒ $60 = \Delta U_{bc} + 0$:. $\Delta U_{\rm hc} = 60 \, \text{J}$ ⇒ (ii) In Process $c \rightarrow a$ Given, $\Delta U_{ca} = -180 \text{ J}$ (iii) Now, for complete cycle, $\Delta U_{abca} = \Delta U_{ab} + \Delta U_{bc} + \Delta U_{ca} = 0$ (iv) From Eqs. (ii), (iii) and (iv), we get $\Delta U_{ab} = -\Delta U_{bc} - \Delta U_{ca}$ $\Delta U_{ab} = -60 + 180 = 120 \text{ J}$(v) From Eq. (i), we get $250 = 120 + \Delta W_{ab}$ $\Rightarrow \Delta W_{ab} = 130 \text{ J}$

Work done by the gas along the path abc, $\Delta W_{abc} = \Delta W_{ab} + \Delta W_{bc} = 130 + 0$ $\Rightarrow \Delta W_{abc} = 130 \text{ J}$

As, work done = Area under the curve Area $_2$ > Area $_1$ > Area $_3$



So, for isobaric process, work done is largest, next for isothermal and then for adiabatic process, \therefore W₂ > W₁ > W₃

115 (a)

Work done, $W_1 = \frac{1}{2} \left(p + \frac{p}{2} \right) V = \frac{3}{4} pV = 0.75 pV$ If the system were taken along the isothermal process,

As $W_1 > W_2$

Thus, statement (a) is correct.

116 (d)

In an isothermal process there is no change of internal energy. Hence RMS velocity remains unchanged.

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117 (b)
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From
$$p_2 V_2^{\gamma} = p_1 V_1^{\gamma}$$

 $\Rightarrow p_2 = p_1 \left(\frac{V_1}{V_2}\right)^{\gamma} = 1 \left(\frac{V_1}{V_1/20}\right)^{1.4}$
 $= 66.28 \text{ atm}$
118 **(b)**
 $\alpha = \frac{Q_2}{W} = \frac{Q_2}{Q_1 - Q_2}$
 $\frac{1}{\alpha} = \frac{Q_1 - Q_2}{Q_2} = \frac{Q_1}{Q_2} - 1$
 $\frac{Q_1}{Q_2} = \frac{1}{\alpha} + 1 = \frac{1 + \alpha}{\alpha}$

α

$$Q_2 = \frac{\alpha Q_1}{1+\alpha}$$